

## Abstract

The interactions between Mars' unique crustal magnetic fields and upper atmospheric electrons, ions and neutrals lead to the formation of currents in the ionospheric dynamo region. These interactions involve elastic and inelastic collisions between ions, electrons and neutrals in the presence of varying pressures, temperatures and densities. The remanent fields embedded in the crust provide Mars with a very rich magnetic topology with significant variations in terms of geometry and magnitude on the order of a few tens to hundreds of kilometers spatially and several orders of magnitude in amplitude. Here we present mesoscale, three-dimensional, multi-fluid, self-consistent simulations of Mars' ionospheric electrodynamics in the dynamo region (~100–400 km altitude), where differential motion of ions and electrons occurs. Our investigations focus on the influence of the magnetic field strength and geometry, and neutral wind speeds, on the dynamo current. We look in particular at the influence of the magnetic field magnitude through simpler, uniform geometries. In addition, our model is able to simulate highly non-uniform magnetic fields involving cusps and loops. To achieve these geometries, we position a small magnetic dipole in the crust and are able to produce representative field configurations. The work presented here investigates the effects of thermospheric neutral winds and magnetic topologies for the dayside ionosphere on the formation and evolution of ionospheric currents on Mars. These simulation predictions will be compared to the data from Mars Atmospheric and Volatile Evolution (MAVEN) mission starting in early 2015. They will ultimately help to assess the ionospheric effects on future missions to the Red Planet.

## I. Introduction

The motivations for our model are as follows:

- Ionospheric composition (e & 71% O<sub>2</sub><sup>+</sup>, 25% CO<sub>2</sub><sup>+</sup>, 4% O<sup>+</sup>) ⇒ multi-fluid model Paty and Winglee [2006]
- Neutral winds ⇒ 3-D model
- Complex magnetic field configuration (Figures 1 & 2) ⇒ systematic validation approach
- 100 km × 50 km × 400 km space scale ⇒ efficient numerical model

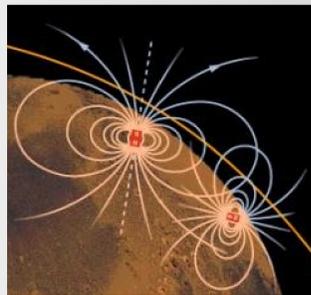


Figure 1: View of Mars' remnant crustal magnetic field. Figure courtesy of Jack Connerney.

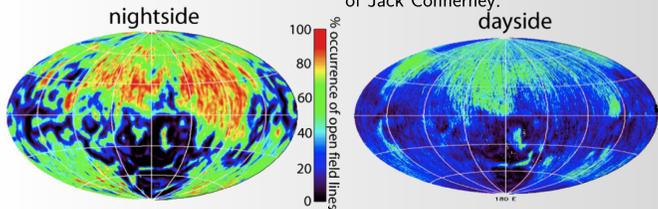


Figure 2: The percent occurrence of open magnetic field lines (i.e. connecting the IMF to the Martian atmosphere) at ~400 km altitude on the nightside and dayside [Brain et al., 2007].

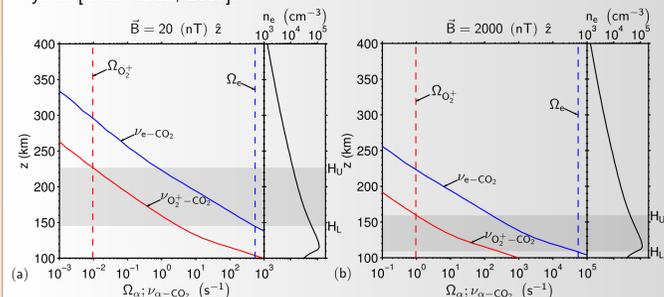


Figure 3: Estimated altitude of the dynamo region for a uniform magnetic field (a)  $\vec{B} = 20 \text{ nT } \hat{z}$ , (b)  $\vec{B} = 2000 \text{ nT } \hat{z}$

## II. Model Formulation

- A 2-step Runge-Kutta method is used [Balay et al., 1997; Pacheco, 1996; Press et al., 1992]
- Neumann boundary conditions are employed
- $i = \text{O}_2^+, \text{CO}_2^+, \text{O}^+$ ;  $e = \text{electron}$

$$\frac{\partial P_i}{\partial t} = -\nabla \cdot (P_i \vec{V}_i) + (\gamma_i - 1) \vec{V}_i \cdot \nabla P_i \quad (1)$$

$$\frac{\partial P_e}{\partial t} = -\nabla \cdot (P_e \vec{V}_e) + (\gamma_e - 1) \vec{V}_e \cdot \nabla P_e \quad (2)$$

$$\rho_i \frac{\partial \vec{V}_i}{\partial t} = -\rho_i (\vec{V}_i \cdot \nabla) \vec{V}_i + e n_i (\vec{E} + \vec{V}_i \times \vec{B}) - \nabla P_i + \frac{\rho_i \vec{g}_M}{(1 + \frac{R_M}{z})^2} \quad (3)$$

$$+ \sum_n \rho_i \nu_{i-n} (\vec{V}_n - \vec{V}_i) \quad (4)$$

$$\vec{V}_e = \sum_i \frac{n_i \vec{V}_i}{n_e} - \frac{\vec{J}}{e n_e} \quad (5)$$

$$\vec{E} = -\vec{V}_e \times \vec{B} - \frac{\nabla P_e}{e n_e} + \frac{m_e}{e} \sum_n \nu_{n-e} (\vec{V}_n - \vec{V}_e) \quad (6)$$

$$\frac{\partial n_i}{\partial t} = -\nabla \cdot (n_i \vec{V}_i) \quad (7)$$

$$\frac{\partial \vec{B}}{\partial t} = -\nabla \times \vec{E} \quad (8)$$

$$\vec{J} = \frac{\nabla \times \vec{B}}{\mu_0} \quad (9)$$

## IV. Uniform Vertical Fields

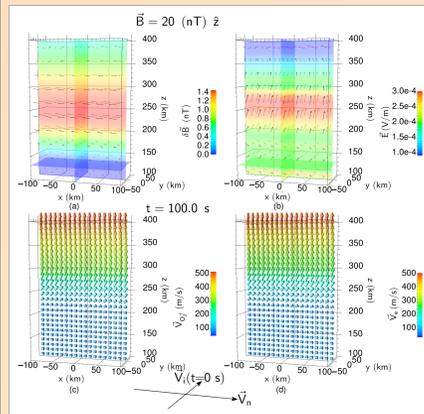


Figure 5: Simulation results at  $t=100.0 \text{ s}$  for  $\vec{B}(t=0)=20 \text{ nT } \hat{z}$ . (a) Magnetic field perturbation  $\delta \vec{B} = \vec{B}(t) - \vec{B}(0)$ ; (b) Electric field; (c) O<sub>2</sub><sup>+</sup> velocity; (d) electron velocities.

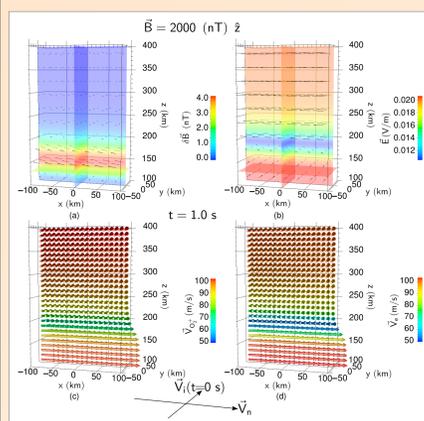


Figure 6: Simulation results at  $t=1.0 \text{ s}$  for  $\vec{B}(t=0)=2000 \text{ nT } \hat{z}$ . (a)-(d) Same as Figure 5.

## III. Initial Conditions

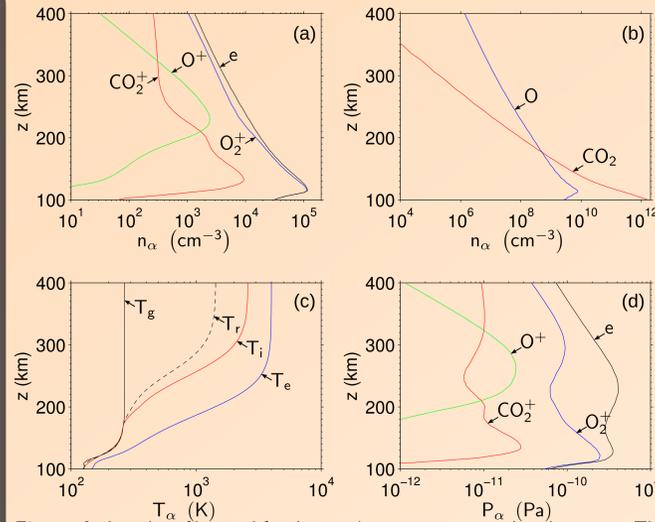


Figure 4: Initial profiles used for the simulation run presented in this paper. The ionization and electron number density profiles are derived from the Mars Climate Database [Lewis et al., 1999] using a photoionization model [Lillis et al., 2012]. The conditions are those of Mars year 24, moderate solar condition, 0° latitude, 0° longitude, Northern autumnal equinox ( $L_S=180^\circ$ ) for 2 PM local time.

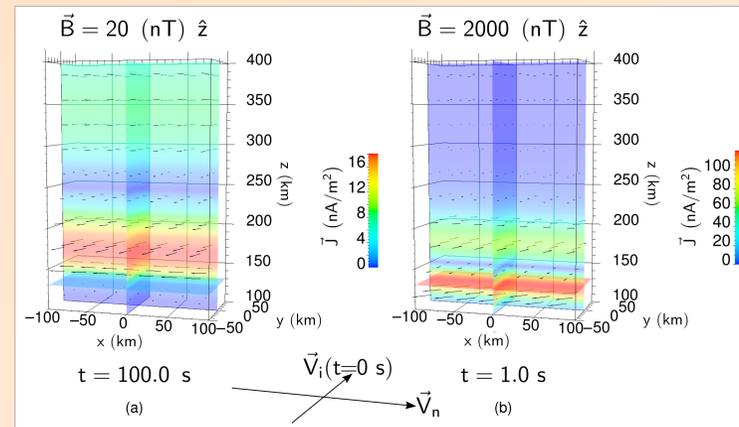


Figure 7:  $\vec{J}$  at  $t=100.0 \text{ s}$  for  $\vec{B}(t=0)=20 \text{ nT } \hat{z}$  (a), and  $t=1.0 \text{ s}$  for  $\vec{B}(t=0)=2000 \text{ nT } \hat{z}$  (b).

Figure 8: Current density components ( $J_x, J_y, J_z$ ) at center of the simulation domain at  $t=100.0 \text{ s}$  for  $\vec{B}(t=0)=20 \text{ nT } \hat{z}$  (a), and  $t=1.0 \text{ s}$  for  $\vec{B}(t=0)=2000 \text{ nT } \hat{z}$  (b). The gray shading emphasizes the location of the dynamo region expected from Figure 3.

Table 1: Maximum dynamo current

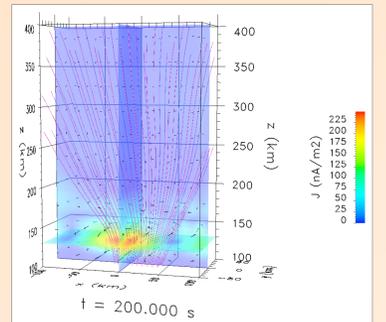
Condition	Ionospheric State	Current Density
$z \gtrsim H_U$	Magnetized ions	$\vec{J}$ small
$H_L \lesssim z \lesssim H_U$	Magnetized electrons	$\vec{J}$ large
	Demagnetized ions	$\vec{J}$ small
	Magnetized electrons	$\vec{J}$ large
$z \lesssim H_L$	Demagnetized ions	$\vec{J}$ small
	Demagnetized electrons	$\vec{J}$ small

- Between  $H_U$  &  $H_L$
- $J_{\max} \approx 2e n_e \vec{V}_n$
- $J_{\max} \propto n_e$  Indirect dependence on  $\vec{B}$
- $J_{\max} \propto \vec{V}_n$  Direct dependence on neutral winds

- Case 1:  $\vec{B} = 20 \text{ nT } \hat{z}$
- $n_e \approx 10^4 \text{ cm}^{-3}$
- $J_{\max} \approx 10^{-7} \text{ A/m}^2$
- Case 2:  $\vec{B} = 2000 \text{ nT } \hat{z}$
- $n_e \approx 10^5 \text{ cm}^{-3}$
- $J_{\max} \approx 10^{-6} \text{ A/m}^2$

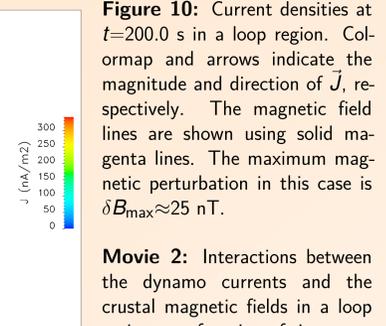
## V. Magnetic Cusps & Loops

Figure 9: Current densities at  $t=200.0 \text{ s}$  in a cusp region. Colormap and arrows indicate the magnitude and direction of  $\vec{J}$ , respectively. The magnetic field lines are shown using solid magenta lines. The maximum magnetic perturbation in this case is  $\delta B_{\max} \approx 12 \text{ nT}$ .



Movie 1: Interactions between the dynamo currents and the crustal magnetic fields in a cusp region as a function of time.

Figure 10: Current densities at  $t=200.0 \text{ s}$  in a loop region. Colormap and arrows indicate the magnitude and direction of  $\vec{J}$ , respectively. The magnetic field lines are shown using solid magenta lines. The maximum magnetic perturbation in this case is  $\delta B_{\max} \approx 25 \text{ nT}$ .



- $|\vec{B}| = 20 \text{ nT}$  @  $z=150 \text{ km}$
- $\vec{V}_n = 100 \text{ m/s } \hat{x}$
- $\vec{V}_\alpha = 100 \text{ m/s } \hat{y}$  @  $t=0 \text{ s}$
- $\vec{J}$  develops around 130 km altitude
- $\delta \vec{B}$  appears
- $\vec{B}$ -field lines get distorted

## VI. Conclusions

The principal results and conclusions developed in this work can be summarized as follows:

- The remanent crustal fields do generate electric currents
- The location of the modeled atmospheric dynamo currents are consistent with those analytically predicted
- The model results for  $\vec{J}_{\max}$  and  $\vec{E}$  are consistent with theoretical calculations
- Mars' ionosphere can be efficiently modeled using a multi-fluid model and therefore our model can be used in more complex geometries
- The 3-D nature of the model is crucial in order to model the structures, currents and fields present in the complex Martian magnetic topology

## References

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